CSC413/2516 Lecture 11: Q-Learning & the Game of Go

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CSC413/2516 Lecture 11: Q-Learning & the

- Reinforcement learning for deep learners
 - Previously, we have seen supervised learning and unsupervised learning with neural networks.
- Today: Q-learning
 - Learn an action-value function that predicts future returns
- Case study: AlphaGo uses both a policy network and a value network

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Overview

- Agent interacts with an environment, which we treat as a black box
- Your RL code accesses it only through an API since it's external to the agent
 - I.e., you're not "allowed" to inspect the transition probabilities, reward distributions, etc.



Recap: Markov Decision Processes

- The environment is represented as a Markov decision process (MDP) *M*.
- Markov assumption: all relevant information is encapsulated in the current state
- Components of an MDP:
 - initial state distribution $p(s_0)$
 - transition distribution $p(s_{t+1} | s_t, a_t)$
 - reward function r(s_t, a_t)
- policy $\pi_{\boldsymbol{\theta}}(\mathsf{a}_t \,|\, \mathsf{s}_t)$ parameterized by $\boldsymbol{\theta}$

• Assume a fully observable environment, i.e. s_t can be observed directly

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Finite and Infinite Horizon

- Last time: finite horizon MDPs
 - Fixed number of steps T per episode
 - Maximize expected return $R = \mathbb{E}_{p(\tau)}[r(\tau)]$
- Now: more convenient to assume infinite horizon
 - We can't sum infinitely many rewards, so we need to discount them: \$100 a year from now is worth less than \$100 today
 - Discounted return

$$G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \cdots$$

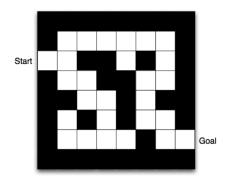
- Want to choose an action to maximize expected discounted return
- The parameter $\gamma < 1$ is called the discount factor
 - small $\gamma = myopic$
 - large $\gamma = farsighted$

Value function V^π(s) of a state s under policy π: the expected discounted return if we start in s and follow π

$$V^{\pi}(\mathsf{s}) = \mathbb{E}[G_t \,|\, \mathsf{s}_t = \mathsf{s}]$$
$$= \mathbb{E}\left[\sum_{i=0}^{\infty} \gamma^i r_{t+i} \,|\, \mathsf{s}_t = \mathsf{s}\right]$$

- Computing the value function is generally impractical, but we can try to approximate (learn) it
- The benefit is credit assignment: see directly how an action affects future returns rather than wait for rollouts

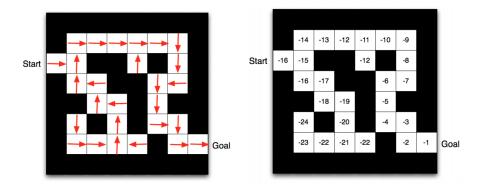
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- Rewards: -1 per time step
- Undiscounted ($\gamma = 1$)
- Actions: N, E, S, W
- State: current location

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• The value function has a recursive formula

$$V^{\pi}(s) = \underset{a_{t},a_{t+i},s_{t+i}}{\mathbb{E}} \left[\sum_{i=0}^{\infty} \gamma^{i} r_{t+i} | s_{t} = s \right]$$
$$= \underset{a_{t}}{\mathbb{E}} \left[r_{t} | s_{t} = s \right] + \gamma \underset{a_{t},a_{t+i},s_{t+i}}{\mathbb{E}} \left[\sum_{i=1}^{\infty} \gamma^{i} r_{t+i+1} | s_{t} = s \right]$$
$$= \underset{a_{t}}{\mathbb{E}} \left[r_{t} | s_{t} = s \right] + \gamma \underset{s_{t+1}}{\mathbb{E}} \left[V^{\pi}(s_{t+1}) | s_{t} = s \right]$$
$$= \underset{a,r}{\sum} P^{\pi}(a|s_{t}) p(r|a,s_{t}) \cdot r + \gamma \underset{a,s'}{\sum} P^{\pi}(a|s_{t}) p(s'|a,s_{t}) \cdot V^{\pi}(s')$$

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Action-Value Function

• Can we use a value function to choose actions?

$$\arg\max_{\mathsf{a}} r(\mathsf{s}_t,\mathsf{a}) + \gamma \mathbb{E}_{p(\mathsf{s}_{t+1}|\mathsf{s}_t,\mathsf{a}_t)}[V^{\pi}(\mathsf{s}_{t+1})]$$

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- Problem: this requires taking the expectation with respect to the environment's dynamics, which we don't have direct access to!
- Instead learn an action-value function, or Q-function: expected returns if you take action a and then follow your policy

$$Q^{\pi}(\mathsf{s},\mathsf{a}) = \mathbb{E}[G_t \,|\, \mathsf{s}_t = \mathsf{s}, \mathsf{a}_t = \mathsf{a}]$$

• Relationship:

$$\mathcal{W}^{\pi}(\mathsf{s}) = \sum_{\mathsf{a}} \pi(\mathsf{a} \,|\, \mathsf{s}) \mathcal{Q}^{\pi}(\mathsf{s},\mathsf{a})$$

Optimal action:

$$\arg \max_{a} Q^{\pi}(s,a)$$

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• The Bellman Equation is a recursive formula for the action-value function:

$$Q^{\pi}(\mathsf{s},\mathsf{a}) = r(\mathsf{s},\mathsf{a}) + \gamma \mathbb{E}_{p(\mathsf{s}'\,|\,\mathsf{s},\mathsf{a})\,\pi(\mathsf{a}'\,|\,\mathsf{s}')}[Q^{\pi}(\mathsf{s}',\mathsf{a}')]$$

• There are various Bellman equations, and most RL algorithms are based on repeatedly applying one of them.

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Optimal Bellman Equation

- The optimal policy π^* is the one that maximizes the expected discounted return, and the optimal action-value function Q^* is the action-value function for π^* .
- The Optimal Bellman Equation gives a recursive formula for Q^* :

$$Q^*(\mathsf{s},\mathsf{a}) = r(\mathsf{s},\mathsf{a}) + \gamma \mathbb{E}_{p(\mathsf{s}' \mid \mathsf{s},\mathsf{a})} \left[\max_{\mathsf{a}'} Q^*(\mathsf{s}_{t+1},\mathsf{a}') \mid \mathsf{s}_t = \mathsf{s}, \mathsf{a}_t = \mathsf{a} \right]$$

• This system of equations characterizes the optimal action-value function. So maybe we can approximate Q^* by trying to solve the optimal Bellman equation!

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Q-Learning

- Let Q be an action-value function which hopefully approximates Q^* .
- The Bellman error is the update to our expected return when we observe the next state s'.

$$\underbrace{r(\mathsf{s}_{t},\mathsf{a}_{t}) + \gamma \max_{\mathsf{a}} Q(\mathsf{s}_{t+1},\mathsf{a})}_{\text{inside } \mathbb{F} \text{ in BHS of Bellman eqn}} - Q(\mathsf{s}_{t},\mathsf{a}_{t})$$

inside \mathbb{E} in RHS of Bellman eqn

- The Bellman equation says the Bellman error is 0 at convergence.
- Q-learning is an algorithm that repeatedly adjusts Q to minimize the Bellman error
- Each time we sample consecutive states and actions (s_t, a_t, s_{t+1}):

$$Q(\mathbf{s}_t, \mathbf{a}_t) \leftarrow Q(\mathbf{s}_t, \mathbf{a}_t) + \alpha \underbrace{\left[r(\mathbf{s}_t, \mathbf{a}_t) + \gamma \max_{\mathbf{a}} Q(\mathbf{s}_{t+1}, \mathbf{a}) - Q(\mathbf{s}_t, \mathbf{a}_t) \right]}_{\text{Bellman error}}$$

Exploration-Exploitation Tradeoff

- Notice: Q-learning only learns about the states and actions it visits.
- Exploration-exploitation tradeoff: the agent should sometimes pick suboptimal actions in order to visit new states and actions.
- Simple solution: *e*-greedy policy
 - With probability 1ϵ , choose the optimal action according to Q
 - With probability ϵ , choose a random action
- Believe it or not, ϵ -greedy is still used today!

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Q-Learning

 $\begin{array}{l} \mbox{Initialize } Q(s,a), \forall s \in \mathbb{S}, a \in \mathcal{A}(s), \mbox{ arbitrarily, and } Q(\textit{terminal-state}, \cdot) = 0 \\ \mbox{Repeat (for each episode):} \\ \mbox{Initialize } S \\ \mbox{Repeat (for each step of episode):} \\ \mbox{Choose } A \mbox{ from } S \mbox{ using policy derived from } Q \mbox{ (e.g., ε-greedy)} \\ \mbox{Take action } A, \mbox{ observe } R, S' \\ Q(S,A) \leftarrow Q(S,A) + \alpha \big[R + \gamma \max_a Q(S',a) - Q(S,A) \big] \\ S \leftarrow S'; \\ \mbox{until } S \mbox{ is terminal} \end{array}$

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Function Approximation

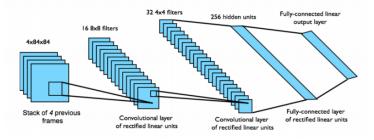
- So far, we've been assuming a tabular representation of *Q*: one entry for every state/action pair.
- This is impractical to store for all but the simplest problems, and doesn't share structure between related states.
- Solution: approximate Q using a parameterized function, e.g.
 - linear function approximation: $Q(s, a) = w^{\top} \psi(s, a)$
 - compute Q with a neural net
- Update Q using backprop:

$$t \leftarrow r(s_t, a_t) + \gamma \max_{a} Q(s_{t+1}, a)$$
$$\theta \leftarrow \theta + \alpha (t - Q(s, a)) \frac{\partial Q}{\partial \theta}$$

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Function Approximation with Neural Networks

- Approximating Q with a neural net is a decades-old idea, but DeepMind got it to work really well on Atari games in 2013 ("deep Q-learning")
- They used a very small network by today's standards



- Main technical innovation: store experience into a replay buffer, and perform Q-learning using stored experience
 - Gains sample efficiency by separating environment interaction from optimization don't need new experience for every SGD update!



- Mnih et al., *Nature* 2015. Human-level control through deep reinforcement learning
- Network was given raw pixels as observations
- Same architecture shared between all games
- Assume fully observable environment, even though that's not the case
- After about a day of training on a particular game, often beat "human-level" performance (number of points within 5 minutes of play)
 - Did very well on reactive games, poorly on ones that require planning (e.g. Montezuma's Revenge)
- https://www.youtube.com/watch?v=V1eYniJORnk
- https://www.youtube.com/watch?v=4MlZncshy1Q

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Wireheading

- If rats have a lever that causes an electrode to stimulate certain "reward centers" in their brain, they'll keep pressing the lever at the expense of sleep, food, etc.
- RL algorithms show this "wireheading" behavior if the reward function isn't designed carefully
- https://blog.openai.com/faulty-reward-functions/

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Policy Gradient vs. Q-Learning

- Policy gradient and Q-learning use two very different choices of representation: policies and value functions
- Advantage of both methods: don't need to model the environment
- Pros/cons of policy gradient
 - Pro: unbiased estimate of gradient of expected return
 - Pro: can handle a large space of actions (since you only need to sample one)
 - Con: high variance updates (implies poor sample efficiency)
 - Con: doesn't do credit assignment
- Pros/cons of Q-learning
 - Pro: lower variance updates, more sample efficient
 - Pro: does credit assignment
 - Con: biased updates since Q function is approximate (drinks its own Kool-Aid)
 - Con: hard to handle many actions (since you need to take the max)

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AlphaGo

- Most of the problem domains we've discussed so far were natural application areas for deep learning (e.g. vision, language)
 - We know they can be done on a neural architecture (i.e. the human brain)
 - The predictions are inherently ambiguous, so we need to find statistical structure
- Board games are a classic AI domain which relied heavily on sophisticated search techniques with a little bit of machine learning
 - Full observations, deterministic environment why would we need uncertainty?
- The second part of the lecture is about AlphaGo, DeepMind's Go playing system which took the world by storm in 2016 by defeating the human Go champion Lee Sedol
- Combines ideas from our last two lectures (policy gradient and value function learning)

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AlphaGo

Some milestones in computer game playing:

- 1949 Claude Shannon proposes the idea of game tree search, explaining how games could be solved algorithmically in principle
- 1951 Alan Turing writes a chess program that he executes by hand
- 1956 Arthur Samuel writes a program that plays checkers better than he does
- 1968 An algorithm defeats human novices at Go

...silence...

- 1992 TD-Gammon plays backgammon competitively with the best human players
- 1996 Chinook wins the US National Checkers Championship
- 1997 DeepBlue defeats world chess champion Garry Kasparov

After chess, Go was humanity's last stand

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- $\bullet\,$ Played on a 19 $\times\,$ 19 board
- Two players, black and white, each place one stone per turn
- Capture opponent's stones by surrounding them



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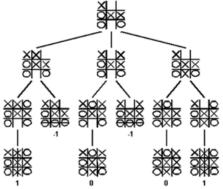
What makes Go so challenging:

- Hundreds of legal moves from any position, many of which are plausible
- Games can last hundreds of moves
- Unlike Chess, endgames are too complicated to solve exactly (endgames had been a major strength of computer players for games like Chess)
- Heavily dependent on pattern recognition

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Game Trees

- Each node corresponds to a legal state of the game.
- The children of a node correspond to possible actions taken by a player.
- Leaf nodes are ones where we can compute the value since a win/draw condition was met



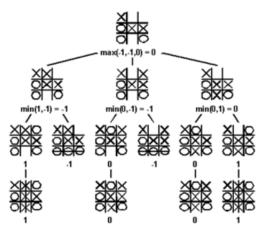
https://www.cs.cmu.edu/~adamchik/15-121/lectures/Game%20Trees/Game%20Trees.html

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Game Trees

• To label the internal nodes, take the max over the children if it's Player 1's turn, min over the children if it's Player 2's turn



https://www.cs.cmu.edu/~adamchik/15-121/lectures/Game%20Trees/Game%20Trees.html

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Game Trees

- As Claude Shannon pointed out in 1949, for games with finite numbers of states, you can solve them in principle by drawing out the whole game tree.
- Ways to deal with the exponential blowup
 - Search to some fixed depth, and then estimate the value using an evaluation function
 - Prioritize exploring the most promising actions for each player (according to the evaluation function)
- Having a good evaluation function is key to good performance
 - Traditionally, this was the main application of machine learning to game playing
 - For programs like Deep Blue, the evaluation function would be a learned linear function of carefully hand-designed features

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Now for DeepMind's computer Go player, AlphaGo...

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Supervised Learning to Predict Expert Moves

• Can a computer play Go without any search?

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Supervised Learning to Predict Expert Moves

- Can a computer play Go without any search?
- Input: a 19 × 19 ternary (black/white/empty) image about half the size of MNIST!
- Prediction: a distribution over all (legal) next moves
- Training data: KGS Go Server, consisting of 160,000 games and 29 million board/next-move pairs
- Architecture: fairly generic conv net
- When playing for real, choose the highest-probability move rather than sampling from the distribution
- This network, which just predicted expert moves, could beat a fairly strong program called GnuGo 97% of the time.
 - This was amazing basically all strong game players had been based on some sort of search over the game tree

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Self-Play and REINFORCE

- The problem from training with expert data: there are only 160,000 games in the database. What if we overfit?
- There is effecitvely infinite data from self-play
 - Have the network repeatedly play against itself as its opponent
 - For stability, it should also play against older versions of itself
- Start with the policy which samples from the predictive distribution over expert moves
 - The network which computes the policy is called the policy network
- **REINFORCE** algorithm: update the policy to maximize the expected reward r at the end of the game (in this case, r = +1 for win, -1 for loss)
- If θ denotes the parameters of the policy network, a_t is the action at time t, and s_t is the state of the board, and z the rollout of the rest of the game using the current policy

$$R = \mathbb{E}_{a_t \sim p_\theta(a_t \mid s_t)} [\mathbb{E}[r(z) \mid s_t, a_t]]$$

Self-Play and REINFORCE

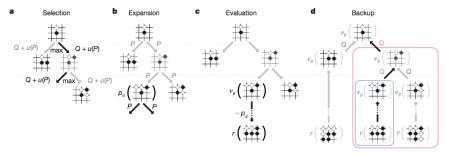
• Gradient of the expected reward:

$$\begin{split} \frac{\partial R}{\partial \theta} &= \frac{\partial R}{\partial \theta} \mathbb{E}_{a_t \sim p_\theta(a_t \mid s_t)} [\mathbb{E}[r(z) \mid s_t, a_t]] \\ &= \frac{\partial}{\partial \theta} \sum_{a_t} \sum_{z} p_\theta(a_t \mid s_t) p(z \mid s_t, a_t) R(z) \\ &= \sum_{a_t} \sum_{z} p(z) R(z) \frac{\partial}{\partial \theta} p_\theta(a_t \mid s_t) \\ &= \sum_{a_t} \sum_{z} p(z \mid s_t, a_t) R(z) p_\theta(a_t \mid s_t) \frac{\partial}{\partial \theta} \log p_\theta(a_t \mid s_t) \\ &= \mathbb{E}_{p_\theta(a_t \mid s_t)} \left[\mathbb{E}_{p(z \mid s_t, a_t)} \left[R(z) \frac{\partial}{\partial \theta} \log p_\theta(a_t \mid s_t) \right] \right] \end{split}$$

- English translation: sample the action from the policy, then sample the rollout for the rest of the game.
 - If you win, update the parameters to make the action more likely. If you lose, update them to make it less likely.

Monte Carlo Tree Search

• In 2006, computer Go was revolutionized by a technique called Monte Carlo Tree Search.



Silver et al., 2016

- Estimate the value of a position by simulating lots of rollouts, i.e. games played randomly using a quick-and-dirty policy
- Keep track of number of wins and losses for each node in the tree
- Key question: how to select which parts of the tree to evaluate?

Jimmy Ba and Bo Wang

CSC413/2516 Lecture 11: Q-Learning & the

Monte Carlo Tree Search

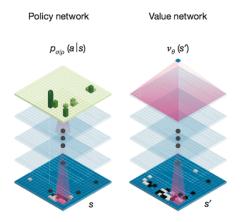
- The selection step determines which part of the game tree to spend computational resources on simulating.
- This is an instance of the exploration-exploitation
 - Want to focus on good actions for the current player
 - But want to explore parts of the tree we're still uncertain about
- Uniform Confidence Bound (UCB) is a common heuristic; choose the node which has the largest frequentist upper confidence bound on its value:

$$\mu_i + \sqrt{\frac{2\log N}{N_i}}$$

• μ_i = fraction of wins for action *i*, N_i = number of times we've tried action *i*, N = total times we've visited this node

Tree Search and Value Networks

- We just saw the policy network. But AlphaGo also has another network called a value network.
- This network tries to predict, for a given position, which player has the advantage.
- This is just a vanilla conv net trained with least-squares regression.
- Data comes from the board positions and outcomes encountered during self-play.



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Silver et al., 2016

Policy and Value Networks

- AlphaGo combined the policy and value networks with Monte Carlo Tree Search
- Policy network used to simulate rollouts
- Value network used to evaluate leaf positions

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AlphaGo Timeline

- Summer 2014 start of the project (internship project for UofT grad student Chris Maddison)
- October 2015 AlphaGo defeats European champion
 - First time a computer Go player defeated a human professional without handicap previously believed to be a decade away
- January 2016 publication of Nature article "Mastering the game of Go with deep neural networks and tree search"
- March 2016 AlphaGo defeats gradmaster Lee Sedol
- October 2017 AlphaGo Zero far surpasses the original AlphaGo without training on any human data
- Decemter 2017 it beats the best chess programs too, for good measure

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AlphaGo

- Most of the Go world expected AlphaGo to lose 5-0 (even after it had beaten the European champion)
- It won the match 4-1
- Some of its moves seemed bizarre to human experts, but turned out to be really good
- Its one loss occurred when Lee Sedol played a move unlike anything in the training data

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AlphaGo

Further reading:

- Silver et al., 2016. Mastering the game of Go with deep neural networks and tree search. *Nature* http://www.nature.com/ nature/journal/v529/n7587/full/nature16961.html
- Scientific American: https://www.scientificamerican.com/ article/how-the-computer-beat-the-go-master/
- Talk by the DeepMind CEO: https://www.youtube.com/watch?v=aiwQsa_7ZIQ&list= PLqYmG7hTraZCGIymT8wVVIXLWkKPNBoFN&index=8

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